

# Indistinguishability of Linear Compartmental Models

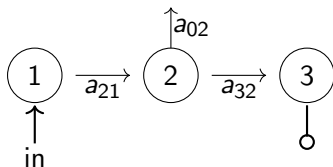
Cash Bortner<sup>\*</sup> and Nicolette Meshkat<sup>†</sup>

<sup>\*</sup>California State University, Stanislaus  
cbortner@csustan.edu

<sup>†</sup>Santa Clara University

Algebraic Systems Biology  
SIAM Conference on Applied Algebraic Geometry, 2025  
University of Wisconsin, Madison, WI  
7/10/2025

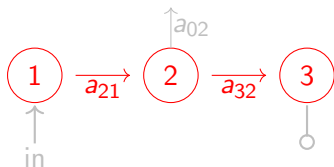
# Motivating Example



## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

# Motivating Example

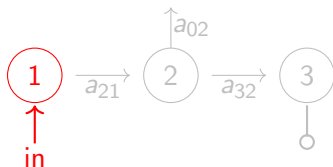


Directed Graph:  $G = \vec{P}_3$

## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (\mathbf{G}, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

# Motivating Example

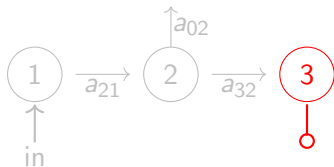


Input Compartment:  $In = \{1\}$

## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, \textcolor{red}{In}, Out, Leak) \\ &= (\vec{P}_3, \textcolor{red}{\{1\}}, \{3\}, \{2\}).\end{aligned}$$

# Motivating Example

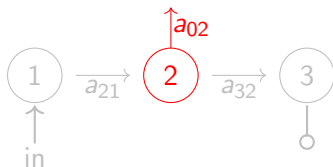


Output Compartment:  $Out = \{3\}$

## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

# Motivating Example



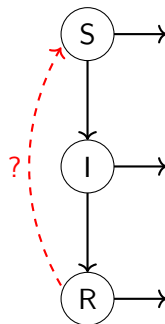
Leak Compartment:  $Leak = \{2\}$

## Linear Compartmental Model

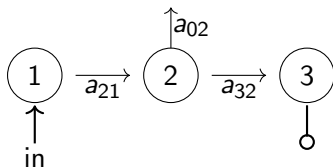
$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

# Compartmental Models in the Wild

- SIR Model for spread of a virus in Epidemiology (non-linear)
- SIV Model for vaccine efficiency in Epidemiology
- Modeling Pharmacokinetics for absorption, distribution, metabolism, and excretion in the blood
- Modeling different biological systems



# Motivating Example

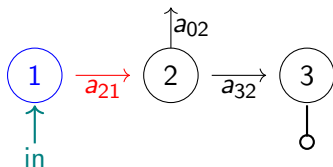


## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$



# Motivating Example



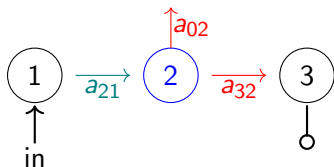
## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

ODEs in terms of concentrations  $x_i(t)$ , input  $u_1(t)$ , and output  $y_3(t)$ :

$$\dot{x}_1(t) = -a_{21}x_1(t) + u_1(t)$$

# Motivating Example



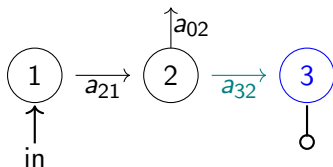
## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

ODEs in terms of concentrations  $x_i(t)$ , input  $u_1(t)$ , and output  $y_3(t)$ :

$$\begin{aligned}\dot{x}_1(t) &= -a_{21}x_1(t) + u_1(t) \\ \dot{x}_2(t) &= a_{21}x_1(t) - (a_{02} + a_{32})x_2(t)\end{aligned}$$

# Motivating Example



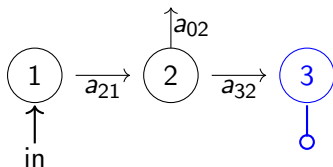
## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

ODEs in terms of concentrations  $x_i(t)$ , input  $u_1(t)$ , and output  $y_3(t)$ :

$$\begin{aligned}\dot{x}_1(t) &= -a_{21}x_1(t) && + u_1(t) \\ \dot{x}_2(t) &= a_{21}x_1(t) - (a_{02} + a_{32})x_2(t) \\ \dot{x}_3(t) &= && a_{32}x_2(t)\end{aligned}$$

# Motivating Example



## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

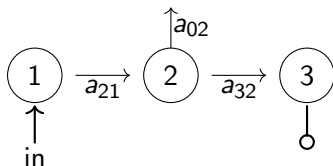
ODEs in terms of concentrations  $x_i(t)$ , input  $u_1(t)$ , and output  $y_3(t)$ :

$$\begin{aligned}\dot{x}_1(t) &= -a_{21}x_1(t) && +u_1(t) \\ \dot{x}_2(t) &= a_{21}x_1(t) - (a_{02} + a_{32})x_2(t) \\ \dot{x}_3(t) &= a_{32}x_2(t)\end{aligned}$$

with

$$y_3(t) = x_3(t).$$

# Motivating Example



## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, In, Out, Leak) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

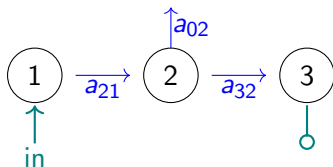
ODEs in terms of concentrations  $x_i(t)$ , input  $u_1(t)$ , and output  $y_3(t)$ :

$$\begin{pmatrix} \dot{x}_1(t) \\ \dot{x}_2(t) \\ \dot{x}_3(t) \end{pmatrix} = \underbrace{\begin{pmatrix} -a_{21} & 0 & 0 \\ a_{21} & -a_{02} - a_{32} & 0 \\ 0 & a_{32} & 0 \end{pmatrix}}_{\text{compartmental matrix } A} \begin{pmatrix} x_1(t) \\ x_2(t) \\ x_3(t) \end{pmatrix} + \begin{pmatrix} u_1(t) \\ 0 \\ 0 \end{pmatrix}$$

with

$$y_3(t) = x_3(t).$$

# Motivating Example: Input/Output Equation



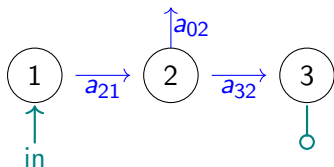
## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, \textit{In}, \textit{Out}, \textit{Leak}) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

Via an application of Cramer's Rule:

$$\det(\partial I - A)y_3 = \overbrace{\det(\partial I - A)^{1,3}}^{\text{remove row 1, col. 3}} u_1$$

# Motivating Example: Input/Output Equation



## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, \text{In}, \text{Out}, \text{Leak}) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

Via an application of Cramer's Rule:

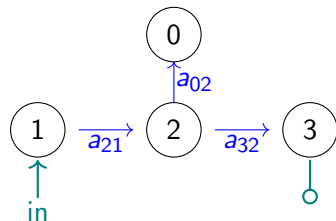
$$\det(\partial I - A)y_3 = \overbrace{\det(\partial I - A)^{1,3}}^{\text{remove row 1, col. 3}} u_1$$

$$y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

an ODE in only the measurable variables and the parameters:

Input/Output Equation

# Motivating Example: Input/Output Equation



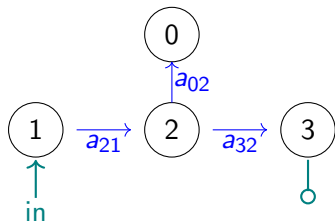
## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, \textit{In}, \textit{Out}, \textit{Leak}) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

$$y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$



# Motivating Example: Input/Output Equation



## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, \text{In}, \text{Out}, \text{Leak}) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

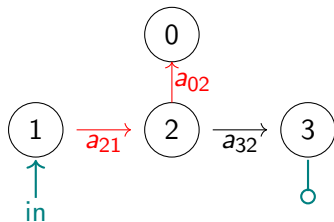
$$y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

### Theorem (\$, Gross, Meshkat, Shiu, Sullivant [2023])

The coefficients of the input-output equation of a LCM  $(G, \text{In}, \text{Out}, \text{Leak})$  can be generated by *incoming forests* on graphs related to  $G$ .

- *incoming*: no vertex has more than **one** outgoing edge
- *forest*: no cycles

# Motivating Example: Input/Output Equation



## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, \text{In}, \text{Out}, \text{Leak}) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

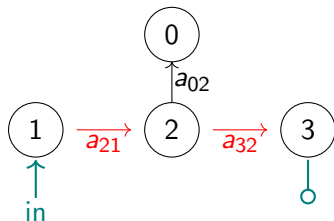
$$y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

### Theorem (\$, Gross, Meshkat, Shiu, Sullivant [2023])

The coefficients of the input-output equation of a LCM  $(G, \text{In}, \text{Out}, \text{Leak})$  can be generated by *incoming forests* on graphs related to  $G$ .

- *incoming*: no vertex has more than **one** outgoing edge
- *forest*: no cycles

# Motivating Example: Input/Output Equation



## Linear Compartmental Model

$$\begin{aligned}\mathcal{M} &= (G, \text{In}, \text{Out}, \text{Leak}) \\ &= (\vec{P}_3, \{1\}, \{3\}, \{2\}).\end{aligned}$$

$$y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

### Theorem (\$, Gross, Meshkat, Shiu, Sullivant [2023])

The coefficients of the input-output equation of a LCM  $(G, \text{In}, \text{Out}, \text{Leak})$  can be generated by *incoming forests* on graphs related to  $G$ .

- *incoming*: no vertex has more than **one** outgoing edge
- *forest*: no cycles

## Motivating Question

How do we know if the model structure we chose which seems to represent the data well is **unique**?

# Indistinguishability

## Motivating Question

How do we know if the model structure we chose which seems to represent the data well is **unique**?

## Definition

Two LCMs are *indistinguishable* if for any choice of parameters in the first model, there is a choice of parameters in the second model that will yield the same *dynamics* in both models.

# Indistinguishability

## Motivating Question

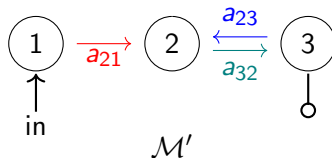
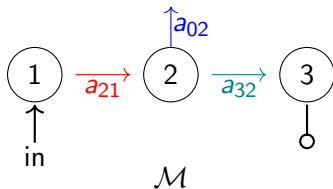
How do we know if the model structure we chose which seems to represent the data well is **unique**?

## Definition

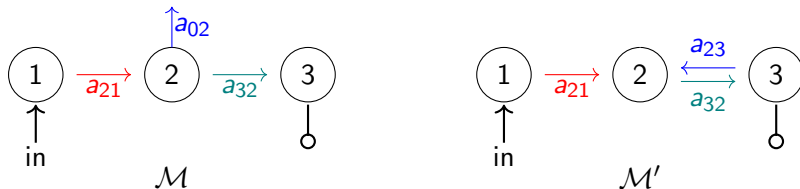
Two LCMs are *indistinguishable* if for any choice of parameters in the first model, there is a choice of parameters in the second model that will yield the same *dynamics* in both models.

What does “same dynamics” mean?

# Motivating Example: Indistinguishability



# Motivating Example: Indistinguishability



$$\mathcal{M} : y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

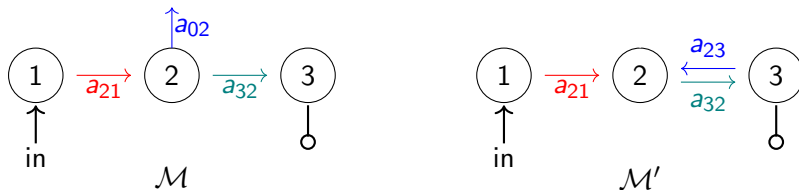
$$\mathcal{M}' : y_3^{(3)} + (a_{21} + a_{23} + a_{32})\ddot{y}_3 + (a_{23}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

## Remark

From the perspective of the input-output equations, we can not *distinguish* between these two very structurally different models.



# Motivating Example: Indistinguishability



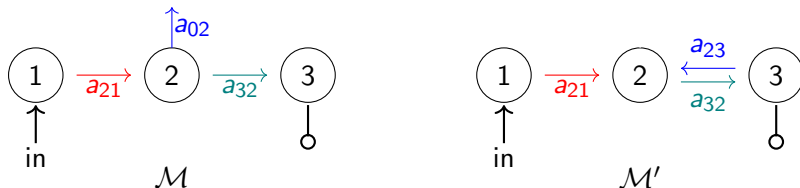
$$\mathcal{M} : y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

$$\mathcal{M}' : y_3^{(3)} + (a_{21} + a_{23} + a_{32})\ddot{y}_3 + (a_{23}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

## Working Definition

Two models are *permutation indistinguishable* if they have the same input-output equations up to renaming the parameters.

# Motivating Example: Indistinguishability

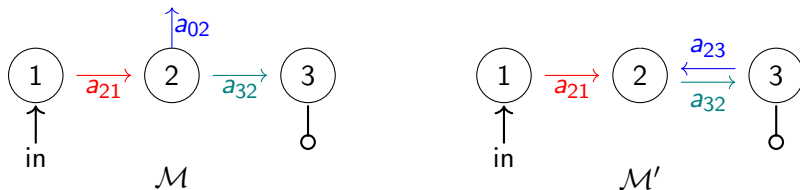


$$\mathcal{M} : y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

$$\mathcal{M}' : y_3^{(3)} + (a_{21} + a_{23} + a_{32})\ddot{y}_3 + (a_{23}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

$$\text{renaming: } \begin{pmatrix} a_{21} \\ a_{02} \\ a_{32} \end{pmatrix} \mapsto \begin{pmatrix} a_{21} \\ a_{23} \\ a_{32} \end{pmatrix}$$

# Motivating Example: Indistinguishability



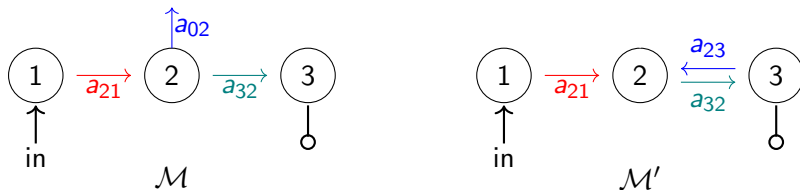
$$\mathcal{M} : y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

$$\mathcal{M}' : y_3^{(3)} + (a_{21} + a_{23} + a_{32})\ddot{y}_3 + (a_{23}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

## Remark

Permutation indistinguishability is an *equivalence relation*!

# Motivating Example: Indistinguishability



$$\mathcal{M} : y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

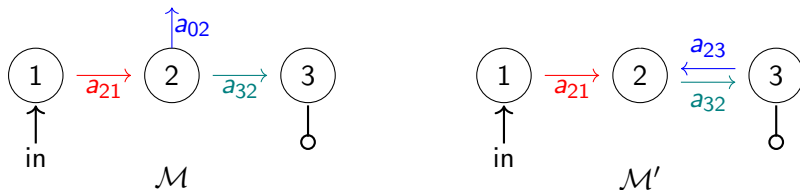
$$\mathcal{M}' : y_3^{(3)} + (a_{21} + a_{23} + a_{32})\ddot{y}_3 + (a_{23}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

## Remark

Permutation indistinguishability is an *equivalence relation*!

**Question:** What is the *equivalence class* of a model?

# Motivating Example: Indistinguishability



$$\mathcal{M} : y_3^{(3)} + (a_{21} + a_{02} + a_{32})\ddot{y}_3 + (a_{02}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

$$\mathcal{M}' : y_3^{(3)} + (a_{21} + a_{23} + a_{32})\ddot{y}_3 + (a_{23}a_{21} + a_{21}a_{32})\dot{y}_3 = (a_{21}a_{32})u_1.$$

## Remark

Permutation indistinguishability is an *equivalence relation*!

**Question:** What is the *equivalence class* of a model? (Size 1?)

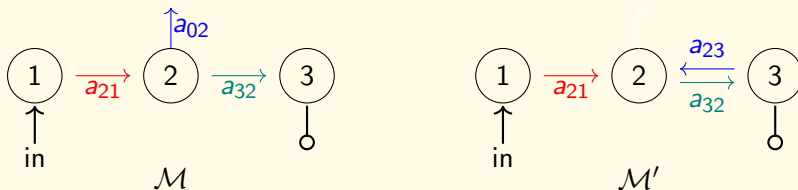
## Previous Work: Necessary Conditions for Indist.

### Theorem (Godfrey & Chapman [1990])

Two indistinguishable models must preserve the following:

1. The length of the shortest path from the input to the output
2. The number of compartments with a path to any output compartment
3. The number of compartments that can be reached from an input
4. The number of traps\*

### Example



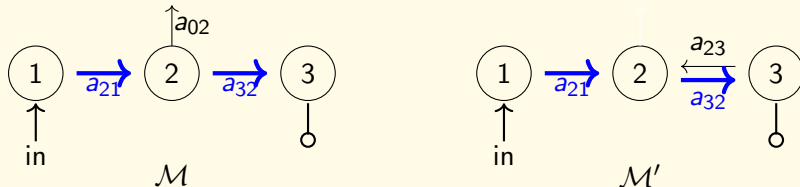
## Previous Work: Necessary Conditions for Indist.

### Theorem (Godfrey & Chapman [1990])

Two indistinguishable models must preserve the following:

1. The length of the shortest path from the input to the output
2. The number of compartments with a path to any output compartment
3. The number of compartments that can be reached from an input
4. The number of traps\*

Example (1.  $\text{Dist}(1, 3) = 2$  in both!)



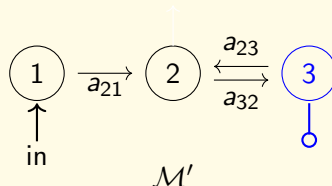
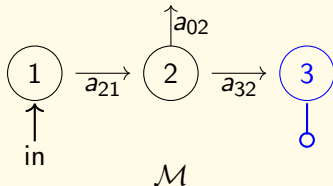
## Previous Work: Necessary Conditions for Indist.

### Theorem (Godfrey & Chapman [1990])

Two indistinguishable models must preserve the following:

1. The length of the shortest path from the input to the output
2. The number of compartments with a path to any output compartment
3. The number of compartments that can be reached from an input
4. The number of traps\*

Example (2. **Two** compartments with a path to the output!)





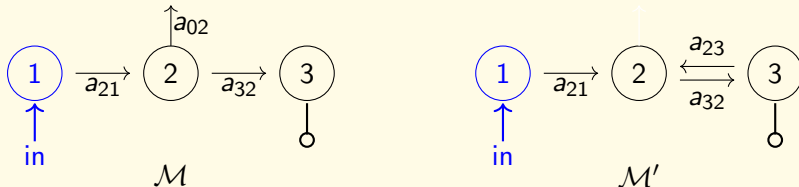
## Previous Work: Necessary Conditions for Indist.

### Theorem (Godfrey & Chapman [1990])

Two indistinguishable models must preserve the following:

1. The length of the shortest path from the input to the output
2. The number of compartments with a path to any output compartment
3. The number of compartments that can be reached from an input
4. The number of traps\*

Example (3. **Two** compartments with a path from the input!)



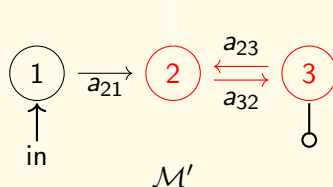
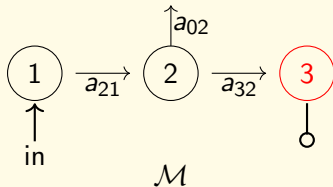
## Previous Work: Necessary Conditions for Indist.

### Theorem (Godfrey & Chapman [1990])

Two indistinguishable models must preserve the following:

1. The length of the shortest path from the input to the output
2. The number of compartments with a path to any output compartment
3. The number of compartments that can be reached from an input
4. The number of traps\*

Example (4. Each model has **one** trap!)



## Previous Work: Necessary Conditions for Indist.

### Theorem (Godfrey & Chapman [1990])

Two indistinguishable models must preserve the following:

1. The length of the shortest path from the input to the output
2. The number of compartments with a path to any output compartment
3. The number of compartments that can be reached from an input
4. The number of traps\*

### Goal:

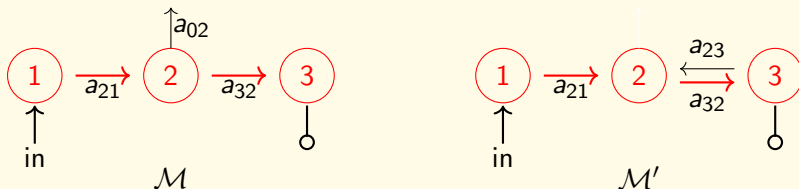
Find *sufficient* conditions for permutation indistinguishability of two models based on their graph structures.

# Skeletal Path Models

## Definition

A *skeletal path model* is an LCM whose graph contains the directed path  $\overrightarrow{P_n}$ , i.e.  $1 \rightarrow 2 \rightarrow \dots \rightarrow n$ , with  $In = \{1\}$  and  $Out = \{n\}$ .

## Example



# Skeletal Path Moves: Walking the Leak

## Question

What *moves* can you perform on a basic skeletal path model resulting in an indistinguishable model?



# Skeletal Path Moves: Walking the Leak

## Question

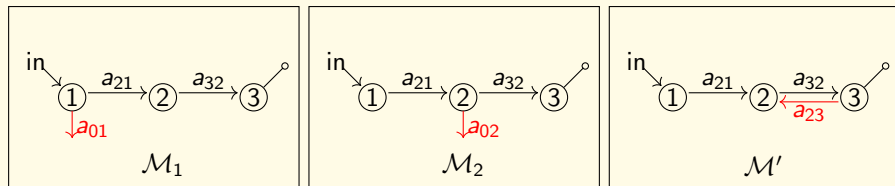
What *moves* can you perform on a basic skeletal path model resulting in an indistinguishable model?

Theorem (§ & Meshkat [2024]; §, Gilliana, Patel, & Tamras [2025\*])

The following skeletal path models are indistinguishable:

- $\mathcal{M}_i = (\vec{P}_n, \{1\}, \{n\}, \{i\})$  for any  $i \in \{1, 2, 3, \dots, n-1\}$
- $\mathcal{M}' = (\vec{P}_n \cup \{n \rightarrow n-1\}, \{1\}, \{n\}, \emptyset)$ .

## Example



# Proof idea

Theorem (§ & Meshkat [2024]; §, Gilliana, Patel, & Tamras [2025\*])

The following skeletal path models are indistinguishable:

- $\mathcal{M}_i = (\vec{P}_n, \{1\}, \{n\}, \{i\})$  for any  $i \in \{1, 2, 3, \dots, n-1\}$
- $\mathcal{M}' = (\vec{P}_n \cup \{n \rightarrow n-1\}, \{1\}, \{n\}, \emptyset)$ .

*Proof idea 1:* Left-hand side of the input/output equation of  $\mathcal{M}_i$  given by:

$$\det(\partial I - A_i)y_n = \det \begin{pmatrix} \partial + a_{21} & 0 & \cdots & \cdots & 0 & 0 \\ -a_{21} & \ddots & \ddots & \ddots & \vdots & \vdots \\ 0 & \ddots & \partial + a_{0i} + a_{i(i-1)} & \ddots & \vdots & \vdots \\ \vdots & \ddots & -a_{i(i-1)} & \ddots & 0 & 0 \\ 0 & \cdots & \ddots & \ddots & \partial + a_{n(n-1)} & 0 \\ 0 & \cdots & \cdots & 0 & -a_{n(n-1)} & \partial \end{pmatrix} y_n$$

# Proof idea

Theorem (§ & Meshkat [2024]; §, Gilliana, Patel, & Tamras [2025\*])

The following skeletal path models are indistinguishable:

- $\mathcal{M}_i = (\vec{P}_n, \{1\}, \{n\}, \{i\})$  for any  $i \in \{1, 2, 3, \dots, n-1\}$
- $\mathcal{M}' = (\vec{P}_n \cup \{n \rightarrow n-1\}, \{1\}, \{n\}, \emptyset)$ .

*Proof idea 2:*

- Under a renaming of the parameters, the incoming forests of each  $\mathcal{M}_i$  are exactly the same as the incoming forests of each  $\mathcal{M}_j$  (and  $\mathcal{M}'$ ).



# Proof idea

Theorem (§ & Meshkat [2024]; §, Gilliana, Patel, & Tamras [2025\*])

The following skeletal path models are indistinguishable:

- $\mathcal{M}_i = (\vec{P}_n, \{1\}, \{n\}, \{i\})$  for any  $i \in \{1, 2, 3, \dots, n-1\}$
- $\mathcal{M}' = (\vec{P}_n \cup \{n \rightarrow n-1\}, \{1\}, \{n\}, \emptyset)$ .

*Proof idea 2:*

- Under a renaming of the parameters, the incoming forests of each  $\mathcal{M}_i$  are exactly the same as the incoming forests of each  $\mathcal{M}_j$  (and  $\mathcal{M}'$ ).
- Thus, each of the coefficients of the respective input/output equations are indistinguishable.

# Detour Models

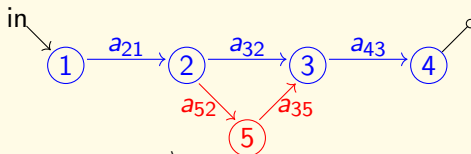
## Definition

A *detour model* is given by

$$\mathcal{M} = (\vec{P}_n \cup D_{i,j}^*, \{1\}, \{n\}, Leak)$$

where  $D$  is some connected directed graph, and  $D_{i,j}^*$  includes one edge from node  $i$  and to node  $j$  in the skeletal path.

## Example



$$\mathcal{M} = (\vec{P}_4 \cup D_{2,3}^*, \{1\}, \{4\}, \emptyset)$$

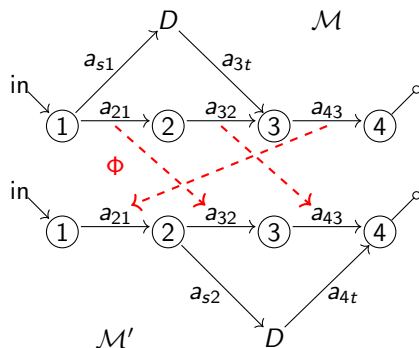
# Detour Models

## Theorem (\$ & Meshkat [2024])

The following two detour models are indistinguishable:

- $\mathcal{M} = (\vec{P}_n \cup D_{i,j}^*, \{1\}, \{n\}, Leak)$
- $\mathcal{M}' = (\vec{P}_n \cup D_{i+1,j+1}^*, \{1\}, \{n\}, Leak)$

*Proof idea:*



- Break the  $A$  matrices into blocks, and show equivalent determinants under  $\Phi$

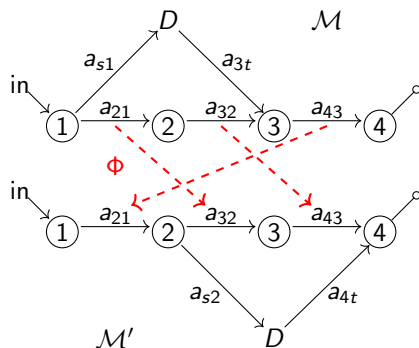
# Detour Models

## Theorem (\$ & Meshkat [2024])

The following two detour models are indistinguishable:

- $\mathcal{M} = (\vec{P}_n \cup D_{i,j}^*, \{1\}, \{n\}, Leak)$
- $\mathcal{M}' = (\vec{P}_n \cup D_{i+1,j+1}^*, \{1\}, \{n\}, Leak)$

*Proof idea:*



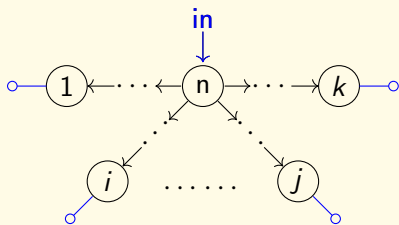
- Break the  $A$  matrices into blocks, and show equivalent determinants under  $\Phi$
- Or, the incoming forests under the renaming  $\Phi$  are the same, so the coefficients are the same!

# Source and Sink Models

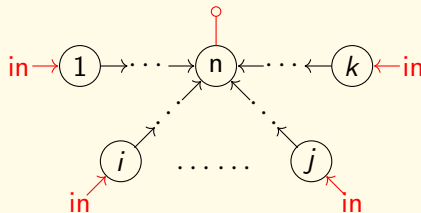
## Corollary (\$ & Meshkat [2024])

We can extend results from detour models to *source* and *sink* models.

### Example



Basic **Source** Model



Basic **Sink** Model

# Future Work

- These are very specific families of LCMs, but this is a proof of concept moving forward!
- More implementation of graph theory in showing sufficient conditions for other families of models
  - Cycle Models (undergraduate research project)
  - Tree Models
- Look into more general indistinguishability from a graph perspective
- Help biologists determine if the model they are using is the **only** model which yield the same dynamics

# References



Cashous Bortner, John Gilliana, Dev Patel, and Zaia Tamras.

Graph theoretic proofs of linear compartmental model indistinguishability.

*Preprint available at <https://arxiv.org/abs/2412.01135>, 2025.*



Cashous Bortner, Elizabeth Gross, Nicolette Meshkat, Anne Shiu, and Seth Sullivan.

Identifiability of linear compartmental tree models and a general formula for the input-output equations.

*Advances in Applied Mathematics*, 146, May 2023.



Cashous Bortner and Nicolette Meshkat.

Graph-based sufficient conditions for the indistinguishability of linear compartmental models.

*SIAM Journal on Applied Dynamical Systems*, 23(3):2179–2207, 2024.



Keith R. Godfrey and Michael J. Chapman.

Identifiability and indistinguishability of linear compartmental models.

*Mathematics and Computers in Simulation*, 32:273–295, 1990.

# Thank you!!!

Partial undergraduate support from the Louis Stokes Alliance for Minority Participation (LSAMP).





# This Presentation!

